

A2.3 A history of evolutionary computation

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Abstract

This section presents a brief but comprehensive summary of the history of evolutionary computation, starting with the ground-breaking work of the 1950s, tracing the rise and development of the three primary forms of evolutionary algorithms (evolution strategies, evolutionary programming and genetic algorithms), and concluding with the present time, in which a more unified view of the field is emerging.

A2.3.1 Introduction

No one will ever produce a completely accurate account of a set of past events since, as someone once pointed out, writing history is as difficult as forecasting. Thus we dare to begin our historical summary of evolutionary computation rather arbitrarily at a stage as recent as the mid-1950s.

At that time there was already evidence of the use of digital computer models to better understand the natural process of evolution. One of the first descriptions of the use of an evolutionary process for computer problem solving appeared in the articles by Friedberg (1958) and Friedberg *et al* (1959). This represented some of the early work in machine learning and described the use of an evolutionary algorithm for *automatic programming*, i.e. the task of finding a program that calculates a given input–output function. Other founders in the field remember a paper of Fraser (1957) that influenced their early work, and there may be many more such forerunners depending on whom one asks.

In the same time frame Bremermann presented some of the first attempts to apply simulated evolution to numerical optimization problems involving both linear and convex optimization as well as the solution of nonlinear simultaneous equations (Bremermann 1962). Bremermann also developed some of the early evolutionary algorithm (EA) theory, showing that the optimal mutation probability for linearly separable problems should have the value of $1/\ell$ in the case of ℓ bits encoding an individual (Bremermann *et al* 1965).

Also during this period Box developed his *evolutionary operation* (EVOP) ideas which involved an evolutionary technique for the design and analysis of (industrial) experiments (Box 1957, Box and Draper 1969). Box's ideas were never realized as a computer algorithm, although Spendley *et al* (1962) used them as the basis for their so-called *simplex design* method. It is interesting to note that the REVOP proposal (Satterthwaite 1959a, b) introducing randomness into the EVOP operations was rejected at that time.

As is the case with many ground-breaking efforts, these early studies were met with considerable skepticism. However, by the mid-1960s the bases for what we today identify as the three main forms of EA were clearly established. The roots of *evolutionary programming* (EP) were laid by Lawrence Fogel [B1.4](#) in San Diego, California (Fogel *et al* 1966) and those of *genetic algorithms* (GAs) were developed at [B1.2](#) the University of Michigan in Ann Arbor by Holland (1967). On the other side of the Atlantic Ocean, *evolution strategies* (ESs) were a joint development of a group of three students, Bienert, Rechenberg, and Schwefel, in Berlin (Rechenberg [B1.3](#) 1965).

Over the next 25 years each of these branches developed quite independently of each other, resulting in unique parallel histories which are described in more detail in the following sections. However, in 1990 there was an organized effort to provide a forum for interaction among the various EA research

communities. This took the form of an international workshop entitled *Parallel Problem Solving from Nature* at Dortmund (Schwefel and Männer 1991).

Since that event the interaction and cooperation among EA researchers from around the world has continued to grow. In the subsequent years special efforts were made by the organizers of *ICGA'91* (Belew and Booker 1991), *EP'92* (Fogel and Atmar 1992), and *PPSN'92* (Männer and Manderick 1992) to provide additional opportunities for interaction.

This increased interaction led to a consensus for the name of this new field, *evolutionary computation* (EC), and the establishment in 1993 of a journal by the same name published by MIT Press. The increasing interest in EC was further indicated by the *IEEE World Congress on Computational Intelligence (WCCI)* at Orlando, Florida, in June 1994 (Michalewicz *et al* 1994), in which one of the three simultaneous conferences was dedicated to EC along with conferences on neural networks and fuzzy systems. The dramatic growth of interest provided additional evidence for the need of an organized EC handbook (which you are now reading) to provide a more cohesive view of the field.

That brings us to the present in which the continued growth of the field is reflected by the many EC events and related activities each year, and its growing maturity reflected by the increasing number of books and articles about EC.

In order to keep this overview brief, we have deliberately suppressed many of the details of the historical developments within each of the three main EC streams. For the interested reader these details are presented in the following sections.

A2.3.2 Evolutionary programming

Evolutionary programming (EP) was devised by Lawrence J Fogel in 1960 while serving at the National Science Foundation (NSF). Fogel was on leave from Convair, tasked as special assistant to the associate director (research), Dr Richard Bolt, to study and write a report on investing in basic research. Artificial intelligence at the time was mainly concentrated around heuristics and the simulation of primitive neural networks. It was clear to Fogel that both these approaches were limited because they model humans rather than the essential process that produces creatures of increasing intellect: evolution. Fogel considered intelligence to be based on adapting behavior to meet goals in a range of environments. In turn, prediction was viewed as the key ingredient to intelligent behavior and this suggested a series of experiments on the use of simulated evolution of *finite-state machines* to forecast nonstationary time series with respect to arbitrary criteria. These and other experiments were documented in a series of publications (Fogel 1962, 1964, Fogel *et al* 1965, 1966, and many others).

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Intelligent behavior was viewed as requiring the composite ability to (i) predict one's environment, coupled with (ii) a translation of the predictions into a suitable response in light of the given goal. For the sake of generality, the environment was described as a sequence of symbols taken from a finite alphabet. The evolutionary problem was defined as evolving an algorithm (essentially a program) that would operate on the sequence of symbols thus far observed in such a manner so as to produce an output symbol that is likely to maximize the algorithm's performance in light of both the next symbol to appear in the environment and a well-defined payoff function. Finite-state machines provided a useful representation for the required behavior.

The proposal was as follows. A population of finite-state machines is exposed to the environment, that is, the sequence of symbols that have been observed up to the current time. For each parent machine, as each input symbol is offered to the machine, each output symbol is compared with the next input symbol. The worth of this prediction is then measured with respect to the payoff function (e.g. all–none, absolute error, squared error, or any other expression of the meaning of the symbols). After the last prediction is made, a function of the payoff for each symbol (e.g. average payoff per symbol) indicates the fitness of the machine.

Offspring machines are created by randomly mutating each parent machine. Each parent produces offspring (this was originally implemented as only a single offspring simply for convenience). There are five possible modes of random mutation that naturally result from the description of the machine: change an output symbol, change a state transition, add a state, delete a state, or change the initial state. The deletion of a state and change of the initial state are only allowed when the parent machine has more than one state. Mutations are chosen with respect to a probability distribution, which is typically uniform. The number of mutations per offspring is also chosen with respect to a probability distribution or may be fixed *a priori*. These offspring are then evaluated over the existing environment in the same manner as

their parents. Other mutations, such as majority logic mating operating on three or more machines, were proposed by Fogel *et al* (1966) but not implemented.

The machines that provide the greatest payoff are retained to become parents of the next generation. (Typically, half the total machines were saved so that the parent population remained at a constant size.) This process is iterated until an actual prediction of the next symbol (as yet unexperienced) in the environment is required. The best machine generates this prediction, the new symbol is added to the experienced environment, and the process is repeated. Fogel (1964) (and Fogel *et al* (1966)) used ‘nonregressive’ evolution. To be retained, a machine had to rank in the best half of the population. Saving lesser-adapted machines was discussed as a possibility (Fogel *et al* 1966, p 21) but not incorporated.

This general procedure was successfully applied to problems in prediction, identification, and automatic control (Fogel *et al* 1964, 1966, Fogel 1968) and was extended to simulate coevolving populations by Fogel and Burgin (1969). Additional experiments evolving finite-state machines for sequence prediction, pattern recognition, and gaming can be found in the work of Lutter and Huntsinger (1969), Burgin (1969), Atmar (1976), Dearholt (1976), and Takeuchi (1980).

In the mid-1980s the general EP procedure was extended to alternative representations including ordered lists for the traveling salesman problem (Fogel and Fogel 1986), and real-valued vectors for continuous function optimization (Fogel and Fogel 1986). This led to other applications in route planning (Fogel 1988, Fogel and Fogel 1988), optimal subset selection (Fogel 1989), and training neural networks (Fogel *et al* 1990), as well as comparisons to other methods of *simulated evolution* (Fogel and Atmar 1990). F1.10
Methods for extending evolutionary search to a two-step process including evolution of the mutation variance were offered by Fogel *et al* (1991, 1992). Just as the proper choice of step sizes is a crucial part of every numerical process, including optimization, the internal adaptation of the mutation variance(s) is of utmost importance for the algorithm’s efficiency. This process is called *self-adaptation* or autoadaptation C7.1
in the case of no explicit control mechanism, e.g. if the variances are part of the individuals’ characteristics and underlie probabilistic variation in a similar way as do the ordinary decision variables.

In the early 1990s efforts were made to organize annual conferences on EP, these leading to the first conference in 1992 (Fogel and Atmar 1992). This conference offered a variety of optimization applications of EP in robotics (McDonnell *et al* 1992, Andersen *et al* 1992), path planning (Larsen and Herman 1992, Page *et al* 1992), *neural network design and training* (Sebald and Fogel 1992, Porto 1992, McDonnell 1992), *automatic control* (Sebald *et al* 1992), and other fields. D1
F1.3

First contacts were made between the EP and ES communities just before this conference, and the similar but independent paths that these two approaches had taken to simulating the process of evolution were clearly apparent. Members of the ES community have participated in all successive EP conferences (Bäck *et al* 1993, Sprave 1994, Bäck and Schütz 1995, Fogel *et al* 1996). There is less similarity between EP and GAs, as the latter emphasize simulating specific mechanisms that apply to natural genetic systems whereas EP emphasizes the behavioral, rather than genetic, relationships between parents and their offspring. Members of the GA and GP communities have, however, also been invited to participate in the annual conferences, making for truly interdisciplinary interaction (see e.g. Altenberg 1994, Land and Belew 1995, Koza and Andre 1996).

Since the early 1990s, efforts in EP have diversified in many directions. Applications in training neural networks have received considerable attention (see e.g. English 1994, Angeline *et al* 1994, McDonnell and Waagen 1994, Porto *et al* 1995), while relatively less attention has been devoted to evolving *fuzzy systems* (Haffner and Sebald 1993, Kim and Jeon 1996). Image processing applications can be found in the articles by Bhattacharjya and Roysam (1994), Brotherton *et al* (1994), Rizki *et al* (1995), and others. Recent efforts to use EP in medicine have been offered by Fogel *et al* (1995) and Gehlhaar *et al* (1995). Efforts studying and comparing methods of self-adaptation can be found in the articles by Saravanan *et al* (1995), Angeline *et al* (1996), and others. Mathematical analyses of EP have been summarized by Fogel (1995). D2

To offer a summary, the initial efforts of L J Fogel indicate some of the early attempts to (i) use simulated evolution to perform prediction, (ii) include variable-length encodings, (iii) use representations that take the form of a sequence of instructions, (iv) incorporate a population of candidate solutions, and (v) coevolve evolutionary programs. Moreover, Fogel (1963, 1964) and Fogel *et al* (1966) offered the early recognition that natural evolution and the human endeavor of the scientific method are essentially similar processes, a notion recently echoed by Gell-Mann (1994). The initial prescriptions for operating on finite-state machines have been extended to arbitrary representations, mutation operators, and selection methods, and techniques for self-adapting the evolutionary search have been proposed and implemented.

The population size need not be kept constant and there can be a variable number of offspring per parent, much like the $(\mu + \lambda)$ methods offered in ESs. In contrast to these methods, selection is often made probabilistic in EP, giving lesser-scoring solutions some probability of surviving as parents into the next generation. In contrast to GAs, no effort is made in EP to support (some say maximize) *schema processing*, nor is the use of random variation constrained to emphasize specific mechanisms of genetic transfer, perhaps providing greater versatility to tackle specific problem domains that are unsuitable for genetic operators such as crossover. C2.4.4
B2.5

A2.3.3 Genetic algorithms

The first glimpses of the ideas underlying genetic algorithms (GAs) are found in Holland's papers in the early 1960s (see e.g. Holland 1962). In them Holland set out a broad and ambitious agenda for understanding the underlying principles of adaptive systems—systems that are capable of self-modification in response to their interactions with the environments in which they must function. Such a theory of adaptive systems should facilitate both the understanding of complex forms of adaptation as they appear in natural systems and our ability to design robust adaptive artifacts.

In Holland's view the key feature of robust natural adaptive systems was the successful use of competition and innovation to provide the ability to dynamically respond to unanticipated events and changing environments. Simple models of biological evolution were seen to capture these ideas nicely via notions of survival of the fittest and the continuous production of new offspring.

This theme of using evolutionary models both to understand natural adaptive systems and to design robust adaptive artifacts gave Holland's work a somewhat different focus than those of other contemporary groups that were exploring the use of evolutionary models in the design of efficient experimental optimization techniques (Rechenberg 1965) or for the evolution of intelligent agents (Fogel *et al* 1966), as reported in the previous section.

By the mid-1960s Holland's ideas began to take on various computational forms as reflected by the PhD students working with Holland. From the outset these systems had a distinct 'genetic' flavor to them in the sense that the objects to be evolved over time were represented internally as 'genomes' and the mechanisms of reproduction and inheritance were simple abstractions of familiar population genetics operators such as mutation, crossover, and inversion.

Bagley's thesis (Bagley 1967) involved tuning sets of weights used in the evaluation functions of game-playing programs, and represents some of the earliest experimental work in the use of diploid representations, the role of inversion, and selection mechanisms. By contrast Rosenberg's thesis (Rosenberg 1967) has a very distinct flavor of simulating the evolution of a simple biochemical system in which single-celled organisms capable of producing enzymes were represented in diploid fashion and were evolved over time to produce appropriate chemical concentrations. Of interest here is some of the earliest experimentation with adaptive crossover operators.

Cavicchio's thesis (Cavicchio 1970) focused on viewing these ideas as a form of adaptive search, and tested them experimentally on difficult search problems involving subroutine selection and pattern recognition. In his work we see some of the early studies on *elitist* forms of selection and ideas for adapting the rates of crossover and mutation. Hollstien's thesis (Hollstien 1971) took the first detailed look at alternate selection and mating schemes. Using a test suite of two-dimensional *fitness landscapes*, he experimented with a variety of breeding strategies drawn from techniques used by animal breeders. Also of interest here is Hollstien's use of binary string encodings of the genome and early observations about the virtues of Gray codings. C2.7.4
B2.7.4

In parallel with these experimental studies, Holland continued to work on a general theory of adaptive systems (Holland 1967). During this period he developed his now famous *schema analysis* of adaptive systems, relating it to the optimal allocation of trials using *k*-armed bandit models (Holland 1969). He used these ideas to develop a more theoretical analysis of his *reproductive plans* (simple GAs) (Holland 1971, 1973). Holland then pulled all of these ideas together in his pivotal book *Adaptation in Natural and Artificial Systems* (Holland 1975). B2.5

Of interest was the fact that many of the desirable properties of these algorithms being identified by Holland theoretically were frequently not observed experimentally. It was not difficult to identify the reasons for this. Hampered by a lack of computational resources and analysis tools, most of the early experimental studies involved a relatively small number of runs using small population sizes (generally

less than 20). It became increasingly clear that many of the observed deviations from expected behavior could be traced to the well-known phenomenon in population genetics of *genetic drift*, the loss of genetic diversity due to the stochastic aspects of selection, reproduction, and the like in small populations.

By the early 1970s there was considerable interest in understanding better the behavior of implementable GAs. In particular, it was clear that choices of population size, representation issues, the choice of operators and operator rates all had significant effects on the observed behavior of GAs. Frantz's thesis (Frantz 1972) reflected this new focus by studying in detail the roles of crossover and inversion in populations of size 100. Of interest here is some of the earliest experimental work on multipoint crossover operators.

De Jong's thesis (De Jong 1975) broadened this line of study by analyzing both theoretically and experimentally the interacting effects of population size, crossover, and mutation on the behavior of a family of GAs being used to optimize a fixed test suite of functions. Out of this study came a strong sense that even these simple GAs had significant potential for solving difficult optimization problems.

The mid-1970s also represented a branching out of the family tree of GAs as other universities and research laboratories established research activities in this area. This happened slowly at first since initial attempts to spread the word about the progress being made in GAs were met with fairly negative perceptions from the artificial intelligence (AI) community as a result of early overhyped work in areas such as self-organizing systems and perceptrons.

Undaunted, groups from several universities including the University of Michigan, the University of Pittsburgh, and the University of Alberta organized an *Adaptive Systems Workshop* in the summer of 1976 in Ann Arbor, Michigan. About 20 people attended and agreed to meet again the following summer. This pattern repeated itself for several years, but by 1979 the organizers felt the need to broaden the scope and make things a little more formal. Holland, De Jong, and Sampson obtained NSF funding for *An Interdisciplinary Workshop in Adaptive Systems*, which was held at the University of Michigan in the summer of 1981 (Sampson 1981).

By this time there were several established research groups working on GAs. At the University of Michigan, Bethke, Goldberg, and Booker were continuing to develop GAs and explore Holland's *classifier systems* as part of their PhD research (Bethke 1981, Booker 1982, Goldberg 1983). At the University of Pittsburgh, Smith and Wetzel were working with De Jong on various GA enhancements including the *Pitt approach* to rule learning (Smith 1980, Wetzel 1983). At the University of Alberta, Brindle continued to look at optimization applications of GAs under the direction of Sampson (Brindle 1981).

The continued growth of interest in GAs led to a series of discussions and plans to hold the first *International Conference on Genetic Algorithms (ICGA)* in Pittsburgh, Pennsylvania, in 1985. There were about 75 participants presenting and discussing a wide range of new developments in both the theory and application of GAs (Grefenstette 1985). The overwhelming success of this meeting resulted in agreement to continue *ICGA* as a biannual conference. Also agreed upon at *ICGA '85* was the initiation of a moderated electronic discussion group called *GA List*.

The field continued to grow and mature as reflected by the *ICGA* conference activities (Grefenstette 1987, Schaffer 1989) and the appearance of several books on the subject (Davis 1987, Goldberg 1989). Goldberg's book, in particular, served as a significant catalyst by presenting current GA theory and applications in a clear and precise form easily understood by a broad audience of scientists and engineers.

By 1989 the *ICGA* conference and other GA-related activities had grown to a point that some more formal mechanisms were needed. The result was the formation of the International Society for Genetic Algorithms (ISGA), an incorporated body whose purpose is to serve as a vehicle for conference funding and to help coordinate and facilitate GA-related activities. One of its first acts of business was to support a proposal to hold a theory workshop on the *Foundations of Genetic Algorithms (FOGA)* in Bloomington, Indiana (Rawlins 1991).

By this time nonstandard GAs were being developed to evolve complex, nonlinear variable-length structures such as rule sets, LISP code, and neural networks. One of the motivations for *FOGA* was the sense that the growth of GA-based applications had driven the field well beyond the capacity of existing theory to provide effective analyses and predictions.

Also in 1990, Schwefel hosted the first *PPSN* conference in Dortmund, which resulted in the first organized interaction between the ES and GA communities. This led to additional interaction at *ICGA '91* in San Diego which resulted in an informal agreement to hold *ICGA* and *PPSN* in alternating years, and a commitment to jointly initiate a journal for the field.

It was felt that in order for the journal to be successful, it must have broad scope and include other species of EA. Efforts were made to include the EP community as well (which began to organize its own conferences in 1992), and the new journal *Evolutionary Computation* was born with the inaugural issue in the spring of 1993.

The period from 1990 to the present has been characterized by tremendous growth and diversity of the GA community as reflected by the many conference activities (e.g. *ICGA* and *FOGA*), the emergence of new books on GAs, and a growing list of journal papers. New paradigms such as *messy GAs* (Goldberg *et al* 1991) and *genetic programming* (Koza 1992) were being developed. The interactions with other EC communities resulted in considerable crossbreeding of ideas and many new hybrid EAs. New GA applications continue to be developed, spanning a wide range of problem areas from engineering design problems to operations research problems to automatic programming. C4.2.4
B1.5.1

A2.3.4 Evolution strategies

In 1964, three students of the Technical University of Berlin, Bienert, Rechenberg, and Schwefel, did not at all aim at devising a new kind of optimization procedure. During their studies of aerotechnology and space technology they met at an Institute of Fluid Mechanics and wanted to construct a kind of research robot that should perform series of experiments on a flexible slender three-dimensional body in a wind tunnel so as to minimize its drag. The method of minimization was planned to be either a one variable at a time or a discrete gradient technique, gleaned from classical numerics. Both strategies, performed manually, failed, however. They became stuck prematurely when used for a two-dimensional demonstration facility, a joint plate—its optimal shape being a flat plate—with which the students tried to demonstrate that it was possible to find the optimum automatically.

Only then did Rechenberg (1965) hit upon the idea to use dice for random decisions. This was the breakthrough—on 12 June 1964. The first version of an evolutionary strategy (ES), later called the $(1 + 1)$ ES, was born, with discrete, binomially distributed mutations centered at the ancestor's position, and just one parent and one descendant per generation. This ES was first tested on a mechanical calculating machine by Schwefel before it was used for the *experimentum crucis*, the joint plate. Even then, it took a while to overcome a merely locally optimal S shape and to converge towards the expected global optimum, the flat plate. Bienert (1967), the third of the three students, later actually constructed a kind of robot that could perform the actions and decisions automatically.

Using this simple *two-membered* ES, another student, Lichtfuß (1965), optimized the shape of a bent pipe, also experimentally. The result was rather unexpected, but nevertheless obviously better than all shapes proposed so far.

First computer experiments, on a Zuse Z23, as well as analytical investigations using binomially distributed integer mutations, had already been performed by Schwefel (1965). The main result was that such a strategy can become stuck prematurely, i.e. at 'solutions' that are not even locally optimal. Based on this experience the use of normally instead of binomially distributed mutations became standard in most of the later computer experiments with real-valued variables and in theoretical investigations into the method's efficiency, but not however in experimental optimization using ESs. In 1966 the little ES community was destroyed by dismissal from the Institute of Fluid Mechanics ('Cybernetics as such is no longer pursued at the institute!'). Not before 1970 was it found together again at the Institute of Measurement and Control of the Technical University of Berlin, sponsored by grants from the German Research Foundation (DFG). Due to the circumstances, the group missed publishing its ideas and results properly, especially in English.

In the meantime the often-cited two-phase nozzle optimization was performed at the Institute of Nuclear Technology of the Technical University of Berlin, then in an industrial surrounding, the AEG research laboratory (Schwefel 1968, Klockgether and Schwefel 1970), also at Berlin. For a hot-water flashing flow the shape of a three-dimensional convergent–divergent (thus supersonic) nozzle with maximum energy efficiency was sought. Though in this experimental optimization an exogenously controlled binomial-like distribution was used again, it was the first time that gene duplication and deletion were incorporated into an EA, especially in a $(1 + 1)$ ES, because the optimal length of the nozzle was not known in advance. As in case of the bent pipe this experimental strategy led to highly unexpected results, not easy to understand even afterwards, but definitely much better than available before.

First Rechenberg and later Schwefel analyzed and improved their ES. For the $(1 + 1)$ ES, Rechenberg, in his Dr.-Ing. thesis of 1971, developed, on the basis of two convex n -dimensional model functions, a

convergence rate theory for $n \gg 1$ variables. Based on these results he formulated a $\frac{1}{5}$ success rule for adapting the standard deviation of mutation (Rechenberg 1973). The hope of arriving at an even better strategy by imitating organic evolution more closely led to the incorporation of the population principle and the introduction of recombination, which of course could not be embedded in the $(1 + 1)$ ES. A first *multimembered* ES, the $(\mu + 1)$ ES—the notation was introduced later by Schwefel—was also designed by Rechenberg in his seminal work of 1973. Because of its inability to self-adapt the mutation step sizes (more accurately, standard deviations of the mutations), this strategy was never widely used.

Much more widespread became the $(\mu + \lambda)$ ES and (μ, λ) ES, both formulated by Schwefel in his Dr.-Ing. thesis of 1974–1975. It contains theoretical results such as a convergence rate theory for the $(1 + \lambda)$ ES and the $(1, \lambda)$ ES ($\lambda > 1$), analogous to the theory introduced by Rechenberg for the $(1 + 1)$ ES (Schwefel 1977). The *multimembered* ($\mu > 1$) ESs arose from the otherwise ineffective incorporation of mutable mutation parameters (variances and covariances of the Gaussian distributions used). Self-adaptation was achieved with the (μ, λ) ES first, not only with respect to the step sizes, but also with respect to correlation coefficients. The enhanced ES version with correlated mutations, described already in an internal report (Schwefel 1974), was published much later (Schwefel 1981) due to the fact that the author left Berlin in 1976. A more detailed empirical analysis of the on-line self-adaptation of the internal or strategy parameters was first published by Schwefel in 1987 (the tests themselves were secretly performed on one of the first small instruction multiple data (SIMD) parallel machines (CRAY1) at the Nuclear Research Centre (KFA) Jülich during the early 1980s with a first parallel version of the multimembered ES with correlated mutations). It was in this work that the notion of *self-adaptation by collective learning* first came up. The importance of recombination (for object as well as strategy parameters) and soft selection (or $\mu > 1$) was clearly demonstrated. Only recently has Beyer (1995a, b) delivered the theoretical background to that particularly important issue.

It may be worth mentioning that in the beginning there were strong objections against increasing λ as well as μ beyond one. The argument against $\lambda > 1$ was that the exploitation of the current knowledge was unnecessarily delayed, and the argument against $\mu > 1$ was that the survival of inferior members of the population would unnecessarily slow down the evolutionary progress. The hint that λ successors could be evaluated in parallel did not convince anybody since parallel computers were neither available nor expected in the near future. The two-membered ES and the very similar creeping random search method of Rastrigin (1965) were investigated thoroughly with respect to their convergence and convergence rates also by Matyas (1965) in Czechoslovakia, Born (1978) on the Eastern side of the Berlin wall (!), and Rappl (1984) in Munich.

Since this early work many new results have been produced by the ES community consisting of the group at Berlin (Rechenberg, since 1972) and that at Dortmund (Schwefel, since 1985). In particular, strategy variants concerning other than only real-valued parameter optimization, i.e. real-world problems, were invented. The first use of an ES for binary optimization using multicellular individuals was presented by Schwefel (1975). The idea of using several subpopulations and *niche mechanisms* for global optimization was propagated by Schwefel in 1977; due to a lack of computing resources, however, it could not be tested thoroughly at that time. Rechenberg (1978) invented a notational scheme for such nested ESs. C6.1

Beside these nonstandard approaches there now exists a wide range of other ESs, e.g. several parallel concepts (Hoffmeister and Schwefel 1990, Lohmann 1991, Rudolph 1991, 1992, Sprave 1994, Rudolph and Sprave 1995), ESs for *multicriterion problems* (Kursawe 1991, 1992), for mixed-integer tasks (Lohmann 1992, Rudolph 1994, Bäck and Schütz 1995), and even for problems with a variable-dimensional parameter space (Schütz and Sprave 1996), and variants concerning nonstandard step size and direction adaptation schemes (see e.g. Matyas 1967, Stewart *et al* 1967, Fürst *et al* 1968, Heydt 1970, Rappl 1984, Ostermeier *et al* 1994). Comparisons between ESs, GAs, and EP may be found in the articles by Bäck *et al* (1991, 1993). It was Bäck (1996) who introduced a common algorithmic scheme for all brands of current EAs. F1.9

Omitting all these other useful nonstandard ESs—a commented collection of literature concerning ES applications was made at the University of Dortmund (Bäck *et al* 1992)—the history of ESs is closed with a mention of three recent books by Rechenberg (1994), Schwefel (1995), and Bäck (1996) as well as three recent contributions that may be seen as written tutorials (Schwefel and Rudolph 1995, Bäck and Schwefel 1995, Schwefel and Bäck 1995), which on the one hand define the actual standard ES algorithms and on the other hand present some recent theoretical results.

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